

Semester 2 Final

Scientific calculators are allowed. Graphing calculators are NOT allowed.

No reference materials (cell phones, notes, book, notecards, or formulas) are allowed during the test.

You must show all your work to receive full credit. Write your answer on the given line.

Chapter 5

(A.REI.6 DOK 2) 3 points

1. Solve the system of linear equations using the substitution method. Write your answer as an ordered pair.

$$\begin{cases} x = -4 - 2y \\ 3x - 4y = 18 \end{cases}$$

$$\begin{aligned} 3(-4 - 2y) - 4y &= 18 & x &= -4 - 2(-3) \\ -12 - 6y - 4y &= 18 & & -4 + 6 \\ -12 - 10y &= 18 & x &= 2 \\ +12 & & & \\ \hline -10y &= 30 \\ y &= -3 \end{aligned}$$

Substitution ~ 1 pt

Solving for x and y ~ 1 pt each

-1/2 point if answer isn't written as an ordered pair

(2, -3)

(A.REI.6 DOK 3) 4 points

2. Solve the system of linear equations using the substitution method. Write your answer as an ordered pair.

$$\begin{cases} 3x - y = 11 \\ 5y - 7x = 1 \end{cases}$$

$$\begin{aligned} 3x - y &= 11 \\ -3x & \quad -3x \\ \hline y &= -3x + 11 \\ y &= 3x - 11 \end{aligned}$$

$$\begin{aligned} 5(3x - 11) - 7x &= 1 & y &= 3(7) - 11 \\ 15x - 55 - 7x &= 1 & y &= 21 - 11 \\ 8x - 55 &= 1 & y &= 10 \\ +55 & & & \\ \hline 8x &= 56 \\ x &= 7 \end{aligned}$$

Solve for a variable ~ 1 pt

Substitution ~ 1 pt

Solving for x and y ~ 1 pt each

-1/2 point if answer isn't written as an ordered pair

(7, 10)

(A.REI.6 DOK 2) 3 points

3. Graph the system by graphing.

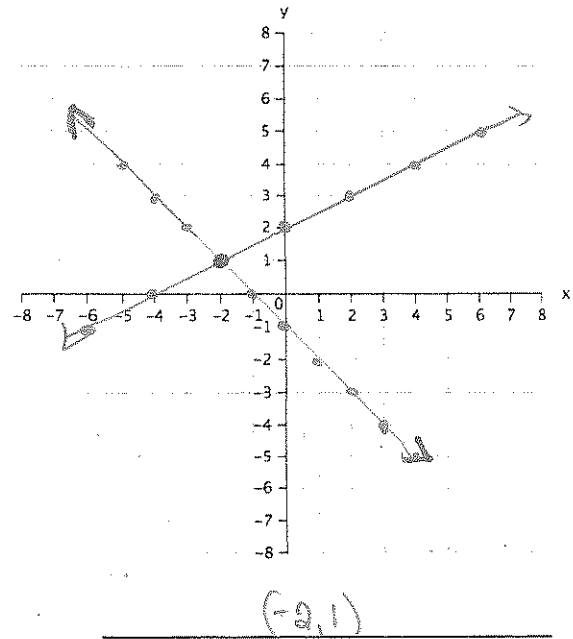
Write your answer as an ordered pair.

$$\begin{cases} y = \frac{1}{2}x + 2 \\ y = -x - 1 \end{cases}$$

Graphing a line ~ 1 pt each

Solution ~ 1 pt

-1/2 pt if not listed as an ordered pair



(A.REI.6 DOK 3) 4 points

4. Graph the system by graphing.

Write your answer as an ordered pair.

$$\begin{cases} x + y = 3 \\ y = -2x - 1 \end{cases}$$

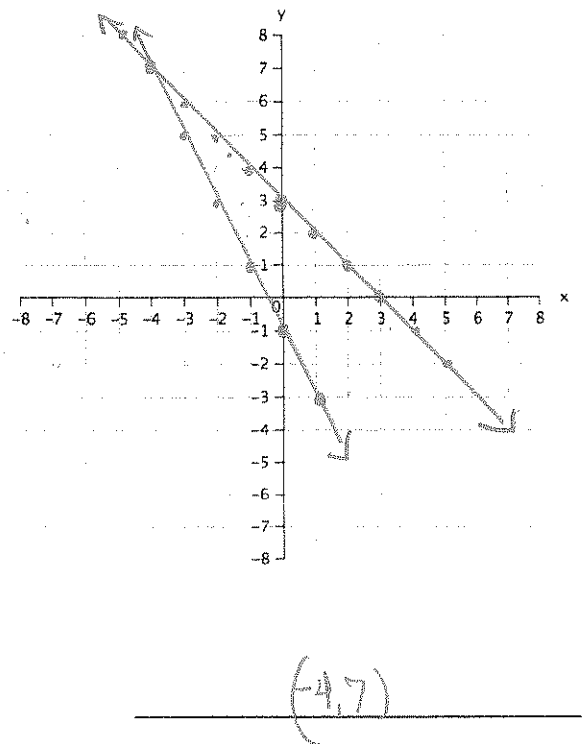
$$\begin{aligned} x + y &= 3 \\ -x & \quad -x \\ \hline y &= -x + 3 \end{aligned}$$

Solve for y ~ 1 pt

Graphing a line ~ 1 pt each

Solution ~ 1 pt

-1/2 pt if not listed as an ordered pair



(A.REI.5 DOK 1) 3 points

5. Solve the system of linear equation using the elimination method. Write your answer as an ordered pair.

$$\begin{cases} x + y = 12 \\ x - y = 2 \end{cases}$$

$2x = 14$ $x = 7$ $7 + y = 12$
Add equations ~ 1 pt
Solve for x and y ~ 2 pts
 -7
 $y = 5$
-1/2 pt for not listing as an ordered pair

(7, 5)

(A.REI.5 DOK 2) 4 points

6. Solve the system of linear equation using the elimination method. Write your answer as an ordered pair.

$$\begin{cases} -(5x + y = 0) \\ 5x + 2y = 30 \end{cases}$$

$$\begin{array}{r} -5x - y = 0 \\ 5x + 2y = 30 \\ \hline 1y = 30 \end{array}$$

$$\begin{array}{r} 5x + 30 = 0 \\ 5x = -30 \\ \hline x = -6 \end{array}$$

Multiply an equation by a constant ~ 1 pt
Add equations ~ 1 pt
Solve for x and y ~ 2 pts
-1/2 pt for not listing as an ordered pair

(-6, 30)

(A.REI.5 DOK 3) 4 points

7. Solve the system of linear equation using the elimination method. Write your answer as an ordered pair.

$$\begin{cases} 2x + 4y = 10 \\ -2(3x + 2y = 17) \end{cases}$$

$$\begin{array}{r} 2x + 4y = 10 \\ -6x - 4y = -34 \\ \hline -4x = -24 \\ \hline x = 6 \end{array}$$

$$\begin{array}{r} 2(6) + 4y = 10 \\ 12 + 4y = 10 \\ \hline 4y = -2 \\ \hline y = -\frac{1}{2} \end{array}$$

Multiply an equation by a constant ~ 1 pt
Add equations ~ 1 pt
Solve for x and y ~ 2 pts
-1/2 pt for not listing as an ordered pair

(6, -1/2)

(A.REI.12 DOK 2) 3 points

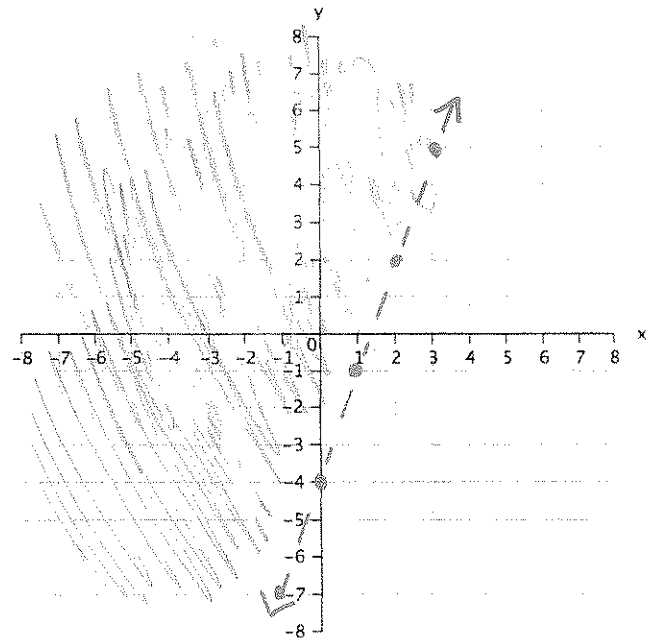
8. Graph the inequality.

$$y > 3x - 4$$

Graphing the line ~ 1 pt

Dotted line ~ 1 pt

Shading ~ 1 pt



(A.REI.12 DOK 2) 6 points

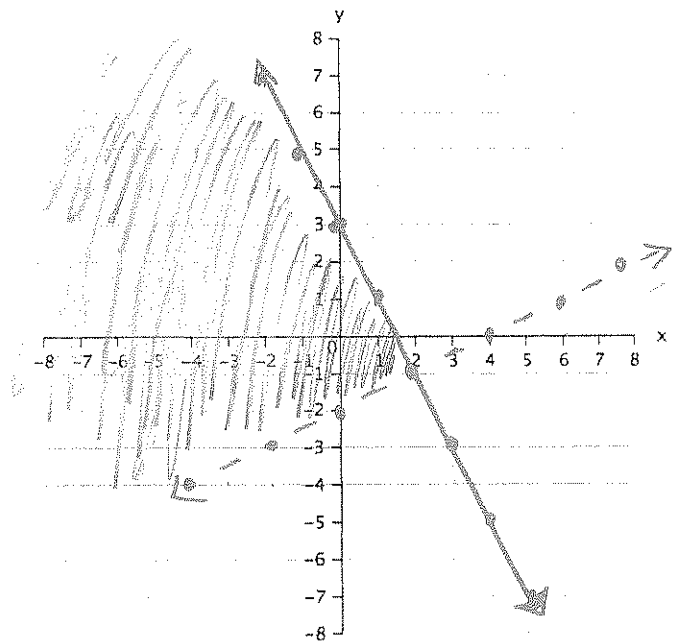
9. Graph the system of inequalities.

$$\begin{cases} y > \frac{1}{2}x - 2 \\ y \leq -2x + 3 \end{cases}$$

Graphing the lines ~ 2 pts

Correct line type ~ 2 pts

Correct shading ~ 2 pts



(A.REI.12 DOK 3) 8 points

10. Graph the system of inequalities.

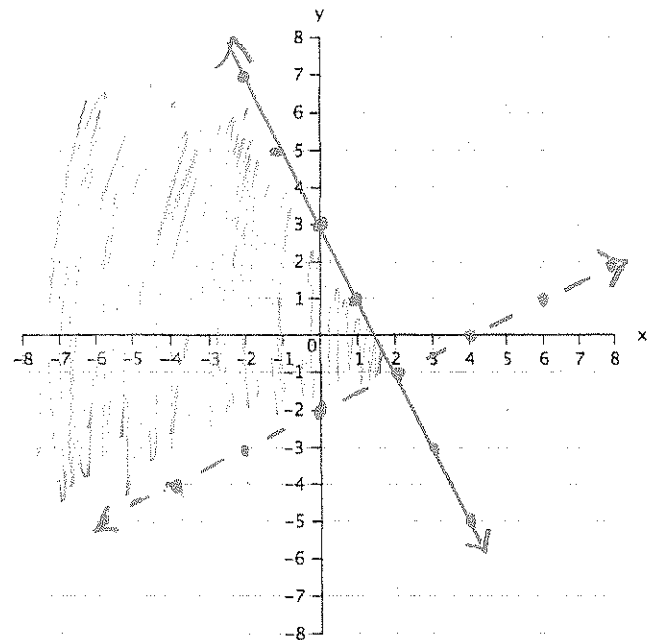
$$\begin{cases} 2x + y \leq 3 \\ x - 2y < 4 \end{cases} \quad y \leq -2x + 3$$

Solve for y ~ 2 pts $y > \frac{1}{2}x - 2$

Graphing the lines ~ 2 pts

Correct line type ~ 2 pts

Correct shading ~ 2 pts



Chapter 6

(A.APR.1 DOK 2) 3 points

11. Simplify.

$$(3b^2 - 2b + 1) - (b^2 - 5b + 4)$$

$$3b^2 - 2b + 1 - b^2 + 5b - 4$$

Distribute the negative ~ 1.5 pts

Combine like terms ~ 1.5 pts

$$\underline{2b^2 + 3b - 3}$$

(A.APR.1 DOK 3) 4 points

12. Simplify.

$$7(2m^2 - 8m) + m(8m + 2) - (3m - 5)$$

$$14m^2 - 56m + 8m^2 + 2m - 3m + 5$$

Distributive ~ 3 pts

Combine like terms ~ 1 pt

$$\underline{22m^2 - 57m + 5}$$

(A.APR.1 DOK 2) 3 points

13. Simplify.

$$5x(7x^2 - x + 4)$$

Distributive ~ 3 pts

$$\underline{35x^3 - 5x^2 + 20x}$$

(A.APR.1 DOK 3) 7 points

14. Simplify.

$$(3x - 2)(4x^2 + 3x - 8)$$

$$12x^3 + 9x^2 - 24x$$

$$- 8x^2 - 6x + 16$$

Distributive 6 times ~ 6 pt

Combine like terms ~ 1 pt

$$\underline{12x^3 + x^2 - 30x + 16}$$

(N.RN.2 DOK 1) 2 points

15. Rewrite the expression with a rational exponent:

$$\sqrt[3]{x^2}$$

$$(x^2)^{1/3} = x^{2/3}$$

Numerator must be 2 ~ 1 pt

Denominator must be 3 ~ 1 pt

$$x^{2/3}$$

(N.RN.2 DOK 1) 2 points

16. Rewrite the expression in radical form:

$$y^{4/5}$$

$$\sqrt[5]{y^4}$$

Index must be 5 ~ 1 pt

Exponent must be 4 ~ 1 pt

$$\sqrt[5]{y^4}$$

(N.RN.2 DOK 2) 3 points

17. Rewrite the expression in radical form:

$$(2x^2)^{2/5}$$

$$\sqrt[5]{(2x^2)^2} = \sqrt[5]{4x^4}$$

Index must be 5 ~ 1 pt

Correct exponent(s) ~ 2 pts

$$\sqrt[5]{4x^4}$$

(N.RN.2 DOK 3) 4 points

18. Simplify and write the answer with rational exponents:

$$\sqrt[4]{x^2y} \cdot \sqrt[4]{xy}$$

$$\sqrt[4]{x^3y^2} = (x^3y^2)^{1/4} = x^{3/4}y^{1/2}$$

Multiplication ~ 2 pts

Converting to rational exponents ~ 2 pts

$$x^{3/4}y^{1/2}$$

(N.RN.2 DOK 3) 4 points

19. Simplify and write the answer in radical form:

$$(2x)^{1/4} \cdot (2x)^{1/2}$$

$$(2x)^{3/4}$$

$$\sqrt[4]{(2x)^3} = \sqrt[4]{8x^3}$$

Multiplication ~ 2 pts

Converting to radical form ~ 2 pts

$$\sqrt[4]{8x^3}$$

Chapter 7

(A.SSE.2 DOK 1) 2 points

20. Factor:

$$6r^2 - 4r$$

Each factor ~ 1 pt

$$\underline{2r(3r - 2)}$$

(A.SSE.2 DOK 2) 3 points

21. Factor:

$$x^2 + 4x - 12$$

Correct signs ~ 1 pt

Correct factors ~ 2 pts

$$\underline{(x + 6)(x - 2)}$$

(A.SSE.2 DOK 2) 3 points

22. Factor:

$$x^2 - 16$$

Correct signs ~ 1 pt

Correct factors ~ 2 pts

$$\underline{(x - 4)(x + 4)}$$

(A.SSE.2 DOK 3) 4 points

23. Factor:

$$5x^2 - 14x + 8$$

Each binomial ~ 2 pts each

$$\begin{array}{l} 40 \cdot 1 \\ 20 \cdot 2 \\ -10 \cdot 4 \end{array}$$

$$5x^2 - 10x - 4x + 8$$

$$5x(x - 2) - 4(x - 2)$$

$$\underline{(x - 2)(5x - 4)}$$

(A.SSE.2 DOK 3) 5 points

24. Factor:

$$3x^3 + 6x^2 - 4x - 8$$

Factor each group ~ 2 pt each

Rewrite as 2 binomials ~ 1 pt

$$\begin{array}{l} 3x^2(x + 2) - 4(x + 2) \\ (3x^2 - 4)(x + 2) \end{array}$$

$$\underline{(3x^2 - 4)(x + 2)}$$

Chapter 8

(A.REI.4b DOK 2) 3 points

25. Solve by taking square roots:

$$2x^2 = 72$$

Divide ~ 1 pt

Square root ~ 1 pt

+/- sign ~ 1 pt

$$\begin{aligned} \frac{2x^2}{2} &= \frac{72}{2} \\ x^2 &= 36 \\ x &= \pm 6 \end{aligned}$$

$$x = \pm 6$$

(A.REI.4b DOK 2) 4 points

26. Solve by factoring:

$$x^2 - 14x + 45 = 0$$

Factor ~ 2 pts

Answers ~ 1 pt each

$$\begin{aligned} (x-9)(x-5) &= 0 \\ x-9 &= 0 & x-5 &= 0 \\ x &= 9 & x &= 5 \end{aligned}$$

$$x = 5, 9$$

(A.REI.4b DOK 3) 5 points

27. Solve using the quadratic formula:

$$2x^2 - 7x + 3 = 0$$

Substitution into formula ~ 2 pts

Discriminant ~ 1 pt

Answers ~ 1 pt each

$$\begin{aligned} 2x^2 - 6x - 1x + 3 &= 0 \\ 2x(x-3) - 1(x-3) &= 0 \\ (2x-1)(x-3) &= 0 \\ \begin{array}{l} 2x-1=0 \\ +1 \quad +1 \\ \hline 2x=1 \\ \frac{2x}{2}=\frac{1}{2} \end{array} & \begin{array}{l} x-3=0 \\ +3 \quad +3 \\ \hline x=3 \end{array} \end{aligned}$$

$$x = \frac{1}{2}, 3$$

(A.REI.4b DOK 3) 6 points

28. Solve by completing the square:

$$2x^2 - 20x + 18 = 0$$

Factor out a 2 ~ 1 pt

Subtract the constant ~ 1 pt

Add 25 to both sides ~ 1 pt

Factor ~ 1 pt

Answer ~ 1 pt each

$$\begin{aligned} \frac{2x^2}{2} - \frac{20x}{2} &= \frac{-18}{2} \\ x^2 - 10x + 25 &= -9 + 25 \\ \left(\frac{-10}{2}\right)^2 &= (-5)^2 = 25 \\ (x-5)^2 &= 16 \\ x-5 &= \pm 4 \end{aligned}$$

$$x = 1, 9$$

$$\begin{array}{l} x-5=4 \\ +5 \quad +5 \\ \hline x=9 \end{array} \quad \begin{array}{l} x-5=-4 \\ +5 \quad +5 \\ \hline x=1 \end{array}$$

Chapter 10

Use the data to answer the following questions 30 – 32.

The finishing times of runners in a 5K race, to the nearest minute, are given.

Finishing Times of Runners in a 5K Race (in minutes)				
18	30	17	17	31
32	19	24	28	22

(S-ID.3 DOK 1) 4 points

29. Find the mean, median, mode and the range.

1 pt each

17, 17, 18, 19, 22, 24, 28, 30, 31, 32
23

Mean: 23.8

Median: 23

Mode: 17

Range: 17-32

(S-ID.3 DOK 2) 3 points

30. A reporter asks you, "What is the typical finishing time for this race?" Which measure of central tendency would you answer: mean or mode? Explain.

Mean ~ 1 pt

Mean, answers will vary.

Explanation ~ 2 pt

(S-ID.3 DOK 3) 4 points

31. Grandma's unofficial time was 68 minutes in the 5K race. If her time was included in the data above, how would this effect the mean, median, mode and range?

Choose one of the following for each: *greatly decreases, slightly decreases, no change, slightly increases, greatly increases*

1 pt each

Mean: ^{or} slight/great Increase \approx (increase 4 mi)

Median: Slight Increase \approx (0.2 min)

Mode: No Change

Range: Greatly increases