# Unit #8 Rotational Motion & Equilibrium

Angular motion, moment of inertia, torque & static equilibrium

Big Idea: Forces can produce torques, and torques can produce rotation.

# **Essential Questions:**

- What causes torque and how is torque defined in terms of a moment arm?
- What effect does a torque have on an object?
- Differentiate between center of mass and center of gravity...
- How is an object's moment of inertia related to changes in its rotation?
- What two kinds of motion are combined in a rolling circular object?

# Vocabulary:

angular position radian average angular velocity center of mass angular speed average angular acceleration moment of inertia momentum arm rotational kinetic energy angular momentum torque

# **Next Generation Priority Standards:**

Students who demonstrate understanding can:

- HS-PS2-1. Analyze data to support the claim that Newton's second law of motion describes the mathematical relationship among the net force on a macroscopic object, its mass, and its acceleration. [Clarification Statement: Examples of data could include tables or graphs of position or velocity as a function of time for objects subject to a net unbalanced force, such as a falling object, an object rolling down a ramp, or a moving object being pulled by a constant force.] [Assessment Boundary: Assessment is limited to one-dimensional motion and to macroscopic objects moving at non-relativistic speeds.]
- HS-PS2-2. Use mathematical representations to support the claim that the total momentum of a system of objects is conserved when there is no net force on the system. [Clarification Statement: Emphasis is on the quantitative conservation of momentum in interactions and the qualitative meaning of this principle.] [Assessment Boundary: Assessment is limited to systems of two macroscopic bodies moving in one dimension.]

- HS-PS3-1. Create a computational model to calculate the change in the energy of one component in a system when the change in energy of the other component(s) and energy flows in and out of the system are known. [Clarification Statement: Emphasis is on explaining the meaning of mathematical expressions used in the model.] [Assessment Boundary: Assessment is limited to basic algebraic expressions or computations; to systems of two or three components; and to thermal energy, kinetic energy, and/or the energies in gravitational, magnetic, or electric fields.]
- HS-PS3-3. Design, build, and refine a device that works within given constraints to convert one form of energy into another form of energy.\*[Clarification Statement: Emphasis is on both qualitative and quantitative evaluations of devices. Examples of devices could include Rube Goldberg devices, wind turbines, solar cells, solar ovens, and generators. Examples of constraints could include use of renewable energy forms and efficiency.] [Assessment Boundary: Assessment for quantitative evaluations is limited to total output for a given input. Assessment is limited to devices constructed with materials provided to students.]

The performance expectations above were developed using the following elements from the NRC document A Framework for K-12 Science Education:

## **Science and Engineering Practices**

### Planning and Carrying Out Investigations

Planning and carrying out investigations to answer questions or test solutions to problems in 9–12 builds on K–8 experiences and progresses to include investigations that provide evidence for and test conceptual, mathematical, physical and empirical models.

## **Analyzing and Interpreting Data**

Analyzing data in 9–12 builds on K–8 and progresses to introducing more detailed statistical analysis, the comparison of data sets for consistency, and the use of models to generate and analyze data.

 Analyze data using tools, technologies, and/or models (e.g., computational, mathematical) in order to make valid and reliable scientific claims or determine an optimal design solution. (HS-PS2-1)

## **Using Mathematics and Computational Thinking**

Mathematical and computational thinking at the 9–12 level builds on K–8 and progresses to using algebraic thinking and analysis, a range of linear and nonlinear functions including trigonometric functions, exponentials and logarithms, and computational tools for statistical analysis to analyze, represent, and model data. Simple computational simulations are created and used based on mathematical models of basic assumptions.

Use mathematical representations of phenomena

## **Disciplinary Core Ideas**

## PS1.A: Structure and Properties of Matter

 The structure and interactions of matter at the bulk scale are determined by electrical forces within and between atoms. (secondary to HS-PS2-6)

#### PS2.A: Forces and Motion

- Newton's second law accurately predicts changes in the motion of macroscopic objects. (HS-PS2-1)
- Momentum is defined for a particular frame of reference; it is the mass times the velocity of the object. (HS-PS2-2)
- If a system interacts with objects outside itself, the total momentum of the system can change; however, any such change is balanced by changes in the momentum of objects outside the system. (HS-PS2-2).

#### PS3.A: Definitions of Energy

- Energy is a quantitative property of a system that depends on the motion and interactions of matter and radiation within that system. That there is a single quantity called energy is due to the fact that a system's total energy is conserved, even as, within the system, energy is continually transferred from one object to another and between its various possible forms. (HS-PS3-1)
- At the macroscopic scale, energy manifests itself in multiple ways, such as in motion, sound, light,

# Crosscutting Concepts

#### Cause and Effect

- Empirical evidence is required to differentiate between cause and correlation and make claims about specific causes and effects. (HS-PS2-1)
- Models can be used to predict the behavior of a system, but these predictions have limited precision and reliability due to the assumptions and approximations inherent in models. (HS-PS3-1)

#### **Systems and System Models**

 When investigating or describing a system, the boundaries and initial conditions of the system need to be defined. (HS-PS2-2)

Connections to Engineering, Technology, and Applications of Science Influence of Science, Engineering and Technology on Society and the Natural World

 Modern civilization depends on major technological systems. Engineers continuously modify these technological systems by applying scientific knowledge and engineering design practices to increase benefits while decreasing costs and risks. (HS-PS3-3)

Connections to Nature of Science
Scientific Knowledge Assumes an Order and

to describe explanations. (HS-PS2-2)

Constructing Explanations and Designing Solutions
Constructing explanations and designing solutions in 9–12
builds on K–8 experiences and progresses to explanations
and designs that are supported by multiple and independent
student-generated sources of evidence consistent with
scientific ideas, principles, and theories.

 Design, evaluate, and/or refine a solution to a complex real-world problem, based on scientific knowledge, student-generated sources of evidence, prioritized criteria, and tradeoff considerations. (HS-PS3-3)

Using Mathematics and Computational Thinking
Mathematical and computational thinking at the 9–12 level
builds on K–8 and progresses to using algebraic thinking and
analysis, a range of linear and nonlinear functions including
trigonometric functions, exponentials and logarithms, and
computational tools for statistical analysis to analyze,
represent, and model data. Simple computational simulations
are created and used based on mathematical models of
basic assumptions.

 Create a computational model or simulation of a phenomenon, designed device, process, or system. (HS-PS3-1)

#### Connections to Nature of Science

Science Models, Laws, Mechanisms, and Theories Explain Natural Phenomena

- Theories and laws provide explanations in science. (HS-PS2-1),
- Laws are statements or descriptions of the relationships among observable phenomena. (HS-PS2-1)

## PS3.B: Conservation of Energy and Energy Transfer

- Conservation of energy means that the total change of energy in any system is always equal to the total energy transferred into or out of the system. (HS-PS3-1)
- Energy cannot be created or destroyed, but it can be transported from one place to another and transferred between systems. (HS-PS3-1)
- Mathematical expressions, which quantify how the stored energy in a system depends on its configuration (e.g. relative positions of charged particles, compression of a spring) and how kinetic energy depends on mass and speed, allow the concept of conservation of energy to be used to predict and describe system behavior. (HS-PS3-1)
- The availability of energy limits what can occur in any system. (HS-PS3-1)

## **PS3.D: Energy in Chemical Processes**

 Although energy cannot be destroyed, it can be converted to less useful forms—for example, to thermal energy in the surrounding environment. (HS-PS3-3)

# ETS1.A: Defining and Delimiting an Engineering Problem

 Criteria and constraints also include satisfying any requirements set by society, such as taking issues of risk mitigation into account, and they should be quantified to the extent possible and stated in such a way that one can tell if a given design meets them. (secondary to HS-PS3-3) Science assumes the universe is a vast single system in which basic laws are consistent. (HS-PS3-1)

Connections to other DCIs in this grade-level:

HS.PS3.A (HS-PS2-4),(HS-PS2-5); HS.PS3.C (HS-PS2-1); HS.PS4.B (HS-PS2-5); HS.ESS1.A (HS-PS2-1)HS.ESS1.C (HS-PS2-1)HS.ESS2.C (HS-PS2-1) HS.ESS3.A

Articulation of DCIs across grade-bands:

MS.PS2.A (HS-PS2-1)(HS-PS2-3); MS.PS3.C (HS-PS2-1),(HS-PS2-2),(HS-PS2-3);

Common Core State Standards Connections:

Connections to other DCIs in this grade-band:

HS.PS1.A (HS-PS3-2); HS.PS1.B (HS-PS3-1),(HS-PS3-2); HS.PS2.B (HS-PS3-2),(HS-PS3-5); HS.LS2.B (HS-PS3-1); HS.ESS1.A (HS-PS3-1),(HS-PS3-4); HS.ESS2.A (HS-PS3-6); HS.ESS2.A (HS-P

1),(HS-PS3-2),(	(HS-PS3-4); <b>HS.ESS2.D</b> (HS-PS3-4); <b>HS.ESS3.A</b> (HS-PS3-3)	
Articulation of L	DCIs across grade-bands:	
MS.PS3.A (HS-	-PS3-1), (HS-PS3-3); <b>MS.PS3.B</b> (HS-PS3-1),(HS-PS3-3) <b>MS.ESS2.A</b> (HS-PS3-1),(HS-PS3-3)	
Common Core	State Standards Connections:	
ELA/Literacy -		
RST.11- 12.1	Cite specific textual evidence to support analysis of science and technical texts, attending to important distinctions the author makes and to any gaps or inconsistencies in the account. (HS-PS3-4)	
WHST.9- 12.7	Conduct short as well as more sustained research projects to answer a question (including a self-generated question) or solve a problem; narrow or broaden the inquir when appropriate; synthesize multiple sources on the subject, demonstrating understanding of the subject under investigation. (HS-PS3-3) HS-PS2-1)	
SL.11-12.5	Make strategic use of digital media (e.g., textual, graphical, audio, visual, and interactive elements) in presentations to enhance understanding of findings, reasoning, and evidence and to add interest. (HS-PS3-1),(HS-PS3-2),	
Mathematics -		
MP.2	Reason abstractly and quantitatively. (HS-PS3-1),(HS-PS3-2),(HS-PS3-3), (HS-PS2-1),(HS-PS2-2)	
MP.4	Model with mathematics. (HS-PS3-1),(HS-PS3-2),(HS-PS2-1),(HS-PS2-2)	
HSN.Q.A.1	Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. (HS-PS3-1),(HS-PS3-3)	
HEN O A 2	Define appropriate quantities for the purpose of descriptive modeling (HC DC2 1) (HC DC2 2)	

Define appropriate quantities for the purpose of descriptive modeling. (HS-PS3-1),(HS-PS3-3)

Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. (HS-PS3-1),(HS-PS3-3)

HSN.Q.A.2 HSN.Q.A.3